MyPL Type Inference Rules. The goal of the following rules are to help clarify type inference and type checking in MyPL. We make the following assumptions.

- The notation e: t says that expression e has type t.
- The **null** value has type **void** (i.e., **null** : **void**) and literals (constants) c have their corresponding type t (i.e., c:t).
- In general, e denotes an expression, t a data type, x a variable/field name, s a struct name, and f a function name.
- Function types are denoted as mappings from parameter type lists (in the order of function parameters) to return types. For example, $f: int, string \rightarrow bool$ says f takes an int and string, and returns a bool.
- Struct types are represented as mappings from field names to types. For example, $s: \{x_1 \to t_1, \dots, x_n \to t_n\}$ says struct s has fields x_1 to x_n with types t_1 to t_n respectively.
- Array types are represented using square brackets, e.g., an int array is denoted as [int].
- Γ is the typing context (environment). The notation $\Gamma \vdash e : t$ says that the current context implies that expression e has type t. Similarly, the notation Γ , stmt $\vdash e : t$ says that the current context extended with the statement implies e has type t. We take some liberties below by assuming we are "in" the statement (stmt) when it extends the scope.
- Unlike syntax rules, the typing rules are meant to provide a guide to some of the details as opposed to an implementation strategy.

Typing Rules for MyPL Expressions:

$$\frac{\Gamma \vdash e_1 : \mathtt{string} \quad \Gamma \vdash e_2 : \mathtt{string}}{\Gamma \vdash e_1 + e_2 : \mathtt{string}} \tag{1}$$

$$\frac{\Gamma \vdash e_1 : t \quad \Gamma \vdash e_2 : t \quad t \in \{\mathsf{int}, \mathsf{double}\} \quad \mathsf{op} \in \{+, -, *, /\}}{\Gamma \vdash e_1 \; \mathsf{op} \; e_2 : t} \tag{2}$$

$$\frac{\Gamma \vdash e_1 : t_1 \quad \Gamma \vdash e_2 : t_2 \quad (t_1 = t_2 \ \lor \ t_1 = \mathtt{void} \ \lor \ t_2 = \mathtt{void}) \quad \mathsf{op} \in \{\texttt{==}, \texttt{!=}\}}{\Gamma \vdash : e_1 \ \mathsf{op} \ e_2 : \mathsf{bool}} \tag{3}$$

$$\frac{\Gamma \vdash e_1 : t \quad \Gamma \vdash e_2 : t \quad t \in \{\text{int,double,string}\} \quad \text{op} \in \{<,>,<=,>=\}}{\Gamma \vdash : e_1 \text{ op} \ e_2 : \text{bool}}$$

$$(4)$$

$$\frac{\Gamma \vdash e_1 : \mathsf{bool} \quad \Gamma \vdash e_2 : \mathsf{bool}}{\Gamma \vdash e_1 \text{ and } e_2 : \mathsf{bool}} \tag{5}$$

$$\frac{\Gamma \vdash e_1 : \mathsf{bool} \quad \Gamma \vdash e_2 : \mathsf{bool}}{\Gamma \vdash e_1 \text{ or } e_2 : \mathsf{bool}} \tag{6}$$

$$\frac{\Gamma \vdash e : \mathsf{bool}}{\Gamma \vdash \mathsf{not} \ e : \mathsf{bool}} \tag{7}$$

Typing Rules for MyPL Statements:

$$\frac{\Gamma \vdash e : t \lor e : \mathbf{void}}{\Gamma, \mathbf{var} \ x : t = e \vdash x : t} \tag{8}$$

$$\frac{\Gamma \vdash e : t \land t \neq \mathsf{void}}{\Gamma, \mathsf{var} \ x = e \vdash x : t} \tag{9}$$

$$\frac{}{\Gamma, \text{var } x: t \vdash x: t} \tag{10}$$

$$\frac{\Gamma \vdash x : t}{\Gamma, \ x = e \vdash e : t \lor e : \mathbf{void}}$$
 (11)

$$\Gamma$$
, while $e \{ \dots \} \vdash e : \mathsf{bool}$ (12)

$$\frac{\Gamma \vdash e_1 : \mathsf{int} \ \land \ e_2 : \mathsf{int}}{\Gamma, \ \mathsf{for} \ x \ \mathsf{from} \ e_1 \ \mathsf{to} \ e_2 \ \{ \dots \} \ \vdash x : \mathsf{int}} \tag{13}$$

$$\overline{\Gamma, \text{if } e \{ \dots \} \vdash e : \text{bool}} \tag{14}$$

$$\overline{\Gamma, \text{if } \{\dots\} \text{ else if } e \{\dots\} \vdash e : \text{bool}}$$
 (15)

Typing Rules for MyPL Structs:

$$\overline{\Gamma, \text{ struct } s \{x_1: t_1, \ldots, x_n: t_n \} \vdash s: \{x_1 \to t_1, \ldots, x_n \to t_n\}}$$

$$(16)$$

$$\frac{\Gamma \vdash e : s \quad \Gamma \vdash s : \{\dots, x_i \to t_i, \dots\}}{\Gamma \vdash e \cdot x_i : t_i}$$
(17)

$$\frac{\Gamma \vdash s : \{x_1 \to t_1, \dots, x_n \to t_n\} \quad \Gamma \vdash e_1 : t_1 \lor e_1 : \mathbf{void} \quad \dots \quad \Gamma \vdash e_n : t_n \lor e_n : \mathbf{void}}{\Gamma \vdash \mathsf{new} \ s(e_1, \dots, e_n) : s} \tag{18}$$

Typing Rules for MyPL Functions:

$$\frac{1}{\Gamma, \ t \ f(x_1: t_1, \ldots, x_n: t_n) \{ \ldots \} \vdash f: t_1, \ldots, t_n \to t}$$

$$\frac{\Gamma \vdash f: t_1, \ldots, t_n \to t \quad \Gamma \vdash e_1: t_1 \lor e_1: \mathsf{void} \cdots \quad \Gamma \vdash e_n: t_n \lor e_n: \mathsf{void}}{\Gamma \vdash f(e_1, \ldots, e_n): t} \tag{20}$$

$$\frac{\Gamma \vdash return : t}{\Gamma, \text{ return } e \vdash e : t \lor e : \text{void}}$$
(21)

Additional Typing Rules for MyPL Arrays:

$$\frac{\Gamma \vdash e : \mathtt{int} \quad t \not\in \{\mathtt{void}, [t']\}}{\Gamma \vdash \mathtt{new} \ t[e] : [t]} \tag{22}$$

$$\frac{\Gamma \vdash e_1 : [t] \quad \Gamma \vdash e_2 : \mathbf{int}}{\Gamma \vdash e_1 [e_2] : t} \tag{23}$$

 $^{^{\}dagger}$ where "return" is a special variable assumed in each function context with the corresponding return type