

Lecture 6:

- Intro to Grammars

Announcements:

- HW-1 out

Formal Grammars

A set of (declarative) rules that define a language's syntax (grammar)

- a “language” here broadly means a set of allowable strings $\{s_1, s_2, \dots\}$
- for this class, the set of allowable programs in a programming language

In PL implementation, grammars can be used within

- Lexers (lexical analysis) e.g., check numbers, strings, comments
- Parsers (syntax analysis) check if syntax is correct

Different “classes” of grammars

- “regular” grammars specify regular languages (think regular expressions)
- “context free” grammars specify context-free languages (most PLs)
- ... and so on
- we'll just cover the basics of regular and context-free grammars

Aside: Grammars are closely tied to computation ...

- If view language of a grammar as output of a program (e.g., binary numbers)
- A grammar exactly “computes” the output
- Here, computing is performed by applying grammar rules to *derive* outputs
- We'll see examples of derivations later

Grammar Rules

Grammar rules define productions (aka rewritings)

$$S \rightarrow a$$

Here we say S produces (or yields) a

- S is a **non-terminal** symbol (LHS of a rule) ... sometimes as $\langle S \rangle$
- a is a **terminal** symbol ... a part of a string
- terminal and non-terminal symbols are disjoint
- set of terminals is the **alphabet** of the language
- often a distinguished **start** symbol

Rules can be applied to create a **derivation** of a string

- from start, repeatedly apply rules until only terminals remain
- we'll see examples soon

Concatenation

$$S \rightarrow ab$$

This says S yields the string consisting of **a** followed by **b**

There can be many ways to define the same language

$$T \rightarrow UV$$

$$U \rightarrow a$$

$$V \rightarrow b$$

Here T yields the same exact language as S (i.e., $\{ab\}$)

Alternation

$$S \rightarrow a \mid b$$

This says S yields the string **a** or **b**

The \mid symbol is special (meta) syntax for separate S -rules:

$$S \rightarrow a$$

$$S \rightarrow b$$

This says S yields the string **a** or S yields the string **b**

The empty string

$$S \rightarrow a \mid \epsilon$$

Where ϵ denotes the special “empty” terminal

This example says S yields either the string a or $''$ (empty string)

Check In: How can this rule be rewritten to not contain alternation?

Kleene Star (Closure)

$$S \rightarrow a^*$$

This says S yields the strings with zero or more a 's

Namely, the strings: $''$, a , aa , aaa , \dots , and in general a^n for $n \geq 0$

Combining Kleene star and concatenation:

$$S \rightarrow a^*b^*$$

This says S yields strings with zero or more a 's followed by zero or more b 's

This is the strings: $''$, a , b , aa , ab , bb , and in general $a^n b^m$ for $n, m \geq 0$

Check In: What is the language defined by the following rule?

$$S \rightarrow a^* \mid b^*$$

Summary – Things to Know

1. Basic grammar rules and terminology (terminals, non-terminals, etc.)
2. Concatenation, Alternation, Empty String, and Kleene Star